



### Profile drag of axisymmetric bodies at zero incidence for subcritical Mach numbers

Associated software: ESDUpac A7819



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#### THE PREPARATION OF THIS DATA ITEM

The work on this particular Data Item which supersedes ESDU Aero B.02.04.01 to 03, was monitored and guided by the Aerodynamics Committee. This Committee first met in 1942 and now has the following membership:

Chairman Mr A.J. Wells	— Independent
Vice-Chairman	
Mr P.D. Chappell	- Independent
Members	
Mr K. Bradbrook	- Independent
Mr P. Camacho <sup>*</sup>	<ul> <li>Boeing, Long Beach, CA, USA</li> </ul>
Dr P.C. Dexter	— Independent
Mr J.R.J. Dovey	— Independent
Prof. K.P. Garry	— Cranfield University
Prof. J.M.R. Graham	<ul> <li>Imperial College, London</li> </ul>
Mr M.J. Green	Independent
Mr J.M. van den Heever	<ul> <li>Denel Dynamics, South Africa</li> </ul>
Dr G.A. Johnson	<ul> <li>BAE SYSTEMS, Advanced Technology Centre, Filton, Bristol</li> </ul>
Dr E.H. Kitchen	<ul> <li>Rolls-Royce Commercial Aero Engines Ltd, Derby</li> </ul>
Mr C.S. Lee	<ul> <li>BAE SYSTEMS, Preston</li> </ul>
Mr JB. Leterrier	<ul> <li>Airbus, Toulouse, France</li> </ul>
Miss M. Maina	<ul> <li>Aircraft Research Association Ltd</li> </ul>
Mr R.S.F. de Mello	— Embraer, Brazil
Mr A. Miller	<ul> <li>Airbus UK, Filton, Bristol</li> </ul>
Mr E. Totland	<ul> <li>— Saab AB, Linköping, Sweden</li> </ul>
Mr J. Tweedie	<ul> <li>Short Brothers plc, Belfast.</li> </ul>

\* Corresponding Member

The members of staff who undertook the technical work involved in the initial assessment of the available information and the construction and subsequent development of the Item were

Mr P.D. Chappell	<ul> <li>— Group Head</li> </ul>
Mr S.F. Wood	<ul> <li>Principal Engineer.</li> </ul>

Subsequent to the issue of ESDU 78019, Addendum A was prepared by Mr P.D. Chappell.

The person with the overall responsibility for the work in this subject area is Mr A.J. Clarke, Head of Aerodynamics Group.

## PROFILE DRAG OF AXISYMMETRIC BODIES AT ZERO INCIDENCE FOR SUBCRITICAL MACH NUMBERS

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### PROFILE DRAG OF AXISYMMETRIC BODIES AT ZERO INCIDENCE FOR SUBCRITICAL MACH NUMBERS

#### 1. NOTATION AND UNITS (see Sketch 1.1)

		SI	British
A	afterbody parameter, $(l_a/D) \tan \tau$		
В	index in expression for flat plate mean skin friction coefficient with fully-turbulent boundary layer, see Equation $(4.3)$		
$C_D$	body profile drag coefficient based on surface area, $D_P/(q_{\infty} \times \pi DLC_S)$		
$C_F$	flat plate mean skin friction coefficient (based on skin friction and area of one side of plate)		
$C_{F0}$	flat plate mean skin friction coefficient (fully-turbulent boundary layer, $x_{tr}/L = 0$ ), see Equation (4.2)		
$C_S$	area coefficient, ratio of body surface area to surface area of enclosing cylinder, $S/(\pi DL)$		
$C_V$	volume (or prismatic) coefficient of body, ratio of body volume to volume of enclosing cylinder, $4V/(\pi D^2 L)$		
C <sub>Va</sub>	volume coefficient of afterbody, $4V_a / (\pi D^2 l_a)$		
$C_{Vf}$	volume coefficient of forebody, $4V_f / (\pi D^2 l_f)$		
D	maximum diameter of body	m	ft
$D_P$	profile drag of body	Ν	lbf
$F_{f}$	correction to correlating parameter $C_S/C_V^n$ to allow for forebody shape and length, see Section 4.2		
$F_{M1}$ , $F_{M2}$	functions of Mach number, see Equations $(4.4)$ and $(4.5)$		
K <sub>M</sub>	correction factor for $M$ , see Equation (4.1)		
K <sub>tr</sub>	correction factor for $x_{tr}/L$ , see Equation (4.1)		
<i>k</i> <sub>1</sub>	family parameter for Body 7 in ESDU 77028		
L	body length	m	ft
l <sub>a</sub>	afterbody length	m	ft
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$l_f$	forebody length	m	ft
l <sub>m</sub>	midbody length	m	ft
M	free-stream Mach number		
п	function of $C_V$ and $D/L$ , see Section 4.2		
$\left. \begin{array}{c} p \\ q \end{array} \right\}$	functions of $l_f (l - C_{Vf})/L$ , see Section 4.3		
$q_{\infty}$	free-stream kinetic pressure	N/m <sup>2</sup>	lbf/ft <sup>2</sup>
R <sub>L</sub>	Reynolds number based on body length		
S	body surface area	m <sup>2</sup>	$\mathrm{ft}^2$
V	body volume	m <sup>3</sup>	$ft^3$
V <sub>a</sub>	afterbody volume	m <sup>3</sup>	$\mathrm{ft}^3$
$V_f$	forebody volume	m <sup>3</sup>	ft <sup>3</sup>
x <sub>tr</sub>	axial distance of boundary-layer transition from nose	m	ft
λ	normalised drag parameter, $C_D/C_F$		
$\lambda_G$	value of $\lambda$ relating to required body at datum boundary-layer and flow conditions, see Section 4.2		
ρ <sub>0</sub>	nose radius of curvature	m	ft
$\bar{\rho}_0$	non-dimensional nose radius, $\rho_0 l_f / D^2$		
τ	tail half-angle	degree	degree



Sketch 1.1 Body geometry

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