API Standard Paragraphs Rotordynamic Tutorial: Lateral Critical Speeds, Unbalance Response, Stability, Train Torsionals, and Rotor Balancing

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1	Scope	1-1
1.1	Introduction	1-1
1.2	Organization	1-1
1.3	Standard Paragraphs	1-2
1.4	Definitions and References	1-3
1.5	Fundamental Concepts of Rotating Equipment Vibrations	1-3
1.6	References	1-9
•	Latend Batandar and a	
2		2-1
2.1		2-1
2.2	Rotor-bearing System Modeling	2-1
2.3	Rotor Modeling Methods and Considerations	2-3
2.4	Support Stiffness Effects	2-15
2.5	Journal Bearings	2-31
2.6	Seal Types and Modeling	2-59
2.7	Elements of a Standard Rotordynamics Analysis	2-77
2.8	Machinery Specific Considerations	2-93
2.9	API Unbalance Response Verification Testing	2-129
2.10	AMB Modeling and Analysis Issues	2-139
3	Stability Analysis	3-1
3.1	Introduction	3-1
3.2	Rotor/Bearing System Modeling	3-5
3.3	Journal Bearings	3-7
3.4	Seals	3-33
3.5	Excitation Sources	3-48
3.6	Support Stiffness Effects on Stability	3-58
3.7	Experience Plots	3-61
3.8	Machinery Specific Considerations	3-68
3.9	Solving Stability Problems	3-86
3.10	Identifving Fluid Induced Instabilities	3-93
3.11	Stability Testing of Machinery	
3.12	Standard Paragraph Sections for Stability Analysis SP6.8.5 – SP6.8.6	
3.13	Active Magnetic Bearings and Stability	
••		
4	Torsional Analysis	4-1
41	General Modeling Considerations	4-1
42	Machinery Specific Modeling Considerations	4-17
4.2	Beciproceting Machinery	4-35
4.0	Torsional Analysis	4-46
7.7 15	Torsional Excitation Sources in Potating Machinery	0+-+ 1-66
4.5		
4.0	Contente of a torsional report	4-70
4./ 10	Tooting to Determine Terrienal Decrement	00-+
4.0	Tersianal Lateral Vibration Counting	4-92
4.9		4-99
4.10	variable Frequency Drives	4-101
5	Balancing of Machinery	5-1
5.1	Introduction	5-1
5.2	Terms and Definitions	5-1

v

5.3	Fundamentals of Low-speed Balancing	5-3
5.4	Low-speed Balancing Machines	5-11
5.5	Low-speed Balancing Procedures	5-16
5.6	Operating-speed Balance	5-24
5.7	Keys and Keyways	5-33
5.8	Residual Unbalance Test	5-33
5.9	Check Balancing	5-34
5.10	Field Balancing	5-34
~	Oten devel Deve were be	C 4
0	Standard Paragraphs	
6.1		6-1
6.2	Paragraphs	6-1
Figu	res	
1-1	Simple Mass-spring-damper System	1-4
1-2	Amplitude Ratio Versus Excitation Frequency	1-6
1-3	Phase Angle Versus Excitation Frequency	1-7
1-4	Response of a Spring-mass System to Transient (Stable)	1-7
1-5	Response of a Spring-mass System to Transient (Unstable)	1-8
1-6	Jeffcott Form for Rotor Model	1-8
1-7	Simplified Model of a Beam-type Rotating Machine	
1-8	Simplified Model of a Beam-type Rotating Machine with Damping	1-10
1-9	Spring-mass-damper Model of Ream Type Rotating Machine	1-10
1-10	Synchronous Response of Ream Type Machine for Various Shaft Stiffness Values	1-11
2-1	Overview of Lateral Analysis Procedure	2-2
2-2	Schematic of a Lumped Parameter Rotor Model	2-4
2-3	3D Finite Element Model of a Complex Geometry Botating Component	2-6
2-0	Elastic Modulus vs. Temperature [4]	2-8
2-5	Botor Model Cross-section of an Fight Stage 12 MW (16 000 HP) Steam Turbine	2_9_0
2-6	Turboeynander with Curvic Counting Fits	∠-5 2_11
2-0	Turbocompressor with Babbet and Curvic Counting Fits	2-11 2-11
2-1 2-8	Modeling of Curvic Coupling Jointe	0_11
2-0	Train Lateral Model	2-11 2_12
2-9	Train Lateral Guideline Diagram $(W_{1,2} - \text{Static Bearing Beaction})$ [5]	2-12 2-12
2-10	Train Lateral Modes	2-12 2-12
2-11	Fauivalent Coupling Model	2-13 2-14
2-12	Steam Turbine Support Schematic	
2-13	Journal Boaring Eluid Film and Elovible Support Model	0_10
2-14	Dynamia Stiffnass Analysis Diagram	2.20
2-15	Exhaust End Dynamic Compliance Plote	2-20
2-10	Single Degree of Freedom Elevible Support Model	2.2-20 2-21
2-17	Stoom End Test Stand Despanse	2.2-21
2-10	Steam End Test Stand Peopeneo	2-25
2-19	Exhaust End Constant Stiffness Summert Model	0.07
2-20	Exhaust End Constant Summess Support Model	0.07
2-21	Steam End Application Depute Dynamic Compliance Model	
2-22	Steam End Analytical Results, Dynamic Compliance Model	
2-23		2-29
2-24		2-31
2-20		2-32
2-26	Spring Sumness	2-33

2-27	Journal Bearing Stiffness and Damping	.2-34
2-28	Pressure Dam Bearing [1]	.2-35
2-29	Pressure Dam Bearing—Top and Bottom Pads [1]	.2-36
2-30	Elliptical Bearing	.2-37
2-31	Offset Half Bearing	.2-37
2-32	Taper Land Bearing with Three Tapered Pockets	.2-38
2-33	Multi-Lobe Bearing with Three Preloaded, Offset Lobes	.2-38
2-34	Five-pad Tilting Pad Bearing Schematic.	.2-41
2-35	Differentiating Load Between Pivots and Load Between Pads	.2-42
2-36	Zero Preloaded Pad	.2-43
2-37	Preloaded Pad	.2-43
2-38	Negative Preloaded Pad	.2-44
2-39	Stiffness and Damping vs. Preload and Bearing Clearance, 4-Pad Bearing [20]	.2-45
2-40	Stiffness and Damping vs. Preload and L/D Ratio, 4-Pad Bearing [20]	.2-46
2-41	Lund's Data vs. Experimental [1]	.2-48
2-42	Jones and Martin Data vs. Experimental [7]	.2-49
2-43	Actual Test Stand Response, 3-Axial Groove Bearings	.2-50
2-44	Analytically Predicted Response for Different Bearing Designs on an Axial Compressor	.2-51
2-45	Actual Test Stand Response, 4-Pad Tilting Pad Bearings	.2-51
2-46	Analytically Predicted Response, Various Bearing Designs	.2-52
2-47	Induction Motor Test Stand Response, Tilting Pad Bearings	.2-53
2-48	Induction Motor Analytical Response, Tilting Pad Bearings	.2-53
2-49	Induction Motor Analytical Response, Elliptical Bearings	.2-54
2-50	Induction Motor Test Stand Response, Elliptical Bearings	.2-54
2-51	Oil Bushing Breakdown Seal	.2-60
2-52	Pressures Experienced by the Outer Floating Ring Seal	.2-61
2-53	Mid-Span Rotor Unbalance Response of a High-pressure Centrifugal Compressor for Different Suc	tion
	Pressures at Start-up [1].	.2-62
2-54	Mechanical (Contact) Shaft Seal	.2-63
2-55	Liquid-film Shaft Seal with Cylindrical Bushing	.2-64
2-56	Liquid-film Shaft Seal with Pumping Bushing	.2-65
2-57	Tilt Pad Oil Seal [2]	.2-66
2-58	Compressor Labyrinth Seals	.2-67
2-59	Typical Turbine Shaft Seal Arrangement—HP End	.2-67
2-60	Honeycomb Damper Seal [32]	.2-68
2-61	Pocket Damper Seal	.2-68
2-62	Hole Pattern Damper Seal with Swirl Brakes [25]	.2-68
2-63	Swirl Brake Used in High-pressure Compressors [26]	.2-69
2-64	Shunt Hole System with Honeycomb Division Wall Seal Used in High-pressure Compressors [30].	.2-69
2-65	Measured Natural Frequency Showing the Increase of the Shaft's First Bending Mode with Pressure [31]	.2-71
2-66	Labyrinth Seal Bulk Flow Control Volume Approaches	.2-71
2-67	Segmented-ring Shaft Seal	.2-73
2-68	Self-acting Dry Gas Seal	.2-74
2-69	Undamped Critical Speed Map	.2-79
2-70	Mode Shape Examples for Soft and Stiff Bearings Relative to Shaft	.2-80
2-71	Typical Regions within an Undamped Critical Speed Map for a Between-Bearing Machine	.2-80
2-72	Typical Undamped Mode Shapes for a Between Bearing Machine with Different Values of Support	
	Stiffness	.2-82
2-73	Typical Bode Plot for Asymmetric System with Split Critical Speeds	.2-85

2-74 Example Compressor with Probes Rotated to True Horizontal and Vertical	
2-75 Evaluating Amplification Factors (AFs) from Speed-amplitude Bode Plots	2-8 8
2-76 Rotor Response Shape Plots in 2D and 3D Form	
2-77 Motion of an Stable System Undergoing Free Oscillations	2-91
2-78 Motion of an Unstable System Undergoing Free Oscillations	2-91
2-79 Integral Shafts Made from a Single Forging	2-94
2-80 Built-up Rotor with Shrunk-on Disks	2-94
2-81 Steam Turbine Outline	2-95
2-82 Typical Resultant Bearing Load Vector Including Partial Admission Steam Forces	
2-83 Sequence of Admission for Different Turbines' Partial Arc Segments	
2-84 Resolution of Partial Admission Forces into Journal Bearing Reactions	
2-85 Induction Motor Rotor	
2-86 Salient Pole Synchronous Motor Rotor	2-100
2-87 Salient Pole Synchronous Motor Rotor	2-101
2-88 Massive Pole Synchronous Motor Rotor	2-102
2-89 Core Magnetic Field Distribution and Cross Section Within a Four Pole Induction Motor [2]	2-102
2-90 Gear Set Showing Rotation Directions	2-105
2-91 Gear Force Schematic	2-106
2-92 Gear Load Angles at Partial and Full Load	2-106
2-93 Accumulated Pitch Error Chart	2-107
2-94 FCC Expander Critical Speed Map	2-109
2-95 FCC Expander Cross-Section	2-111
2-96 FCC Expander Rotor-bearing Support Model	2-112
2-97 Axial Compressor Rotor Construction: Disc-on-shaft Shrink Fit	2-113
2-98 Axial Compressor Rotor Construction: Stacked Discs with Tie Bolts	2-114
2-99 Axial Compressor Rotor Construction: Drum Rotor with Studs	2-114
2-100 Axial Compressor Rotor Construction: Drum Rotor with Tie Bolts	2-115
2-101 Typical Multi-stage Compressor	2-116
2-102 Soft Support Undamped Mode Shapes—Multi-stage Compressor	2-117
2-103 Stiff Support Undamped Mode Shapes—Multi-stage Compressor	2-118
2-104 Typical Unbalance Distributions for Multi-stage Compressors	2-118
2-105 Unbalance Response of 1st and 3rd Critical Speeds	2-119
2-106 Rotor Response Shape @ 4500 rpm	2-119
2-107 Unbalance Response of 2nd Critical Speed.	2-120
2-108 Rotor Response Shape @ 12,800 rpm	2-120
2-109 Typical Overhung Compressor 2-121	
2-110 Overhung Compressor Assembly	2-122
2-111 Overhung Compressor Undamped Mode Shapes (Impeller on Right)	2-123
2-112 Undamped Critical Speed Map—Overhung Compressor	2-124
2-113 Impeller Unbalance Response—Overhung Compressor	2-125
2-114 Rotor Response Shape at 4,300 rpm	2-125
2-116 Integrally Geared Compressor Cross-Section	2-126
2-115 Coupling Unbalance Response—Overhung Compressors	2-126
2-117 View of Integrally Geared Compressor Assembly	2-127
2-118 Typical Pinion Rotors from an Integrally Geared Compressor	2-128
2-119 Pinion Rotor Model—Integrally Geared Compressor	2-128
2-120 Typical Rigid and Flexible Body Mode Shapes & Unbalances Used to Excite Each	2-129
2-121 Baseline Vibration Reading (Graphically)	2-133
2-122 Readings After the Addition of the Unbalance Weight	2-133

2-123 Influence of the Unbalance Weight	.2-134
2-124 Bode Plot for Eight-Stage Compressor [1]	.2-135
2-125 Unbalance Weight Influence (Predicted Test) [1]	.2-135
2-126 Bode Plot for Three-Stage Compressor [1]	2-136
2-127 Unbalance Weight Influence (Predicted Test) [1]	.2-136
2-128 Bode Plot of Example #3 [1]	2-137
2-129 Unbalance Weight Influence [1]	.2-138
2-130 AMB System 2-139	
2-131 AMB System Radial Axes	2-140
2-132 SISO Control	.2-143
2-133 SISO Control Transfer Function Matrix	2-143
2-134 MIMO Control	2-144
2-135 Transfer Function Matrix for MIMO Control (General Case)	2-144
2-136 Typical Control System Transfer Function Bode Plot	2-145
2-137 Typical Ereq. Freq AMB Man ($N = 30.000$ BPM)	2-143 2-147
2-138 AMB Force Limitations	2-140
2 120 Typical AMB Allowable Earce Envelope	2-149
2-139 Typical AMB Allowable Force Envelope	0 150
2-140 Closed Loop Transler Function Measurement Locations	0 152
2-141 Example AMD Closed Loop Transfer Function	.2-155
2-142 Open Loop Transfer Function.	2-155
2-143 Typical Open Loop Transfer Function Measurement for Most Controlled Systems	.2-154
2-144 Practical "Pseudo Open Loop" Transfer Function Measurement for AMB System	.2-154
2-145 Example Pseudo Open Loop Transfer Function 2-155	0 4 5 7
2-146 Closed Loop Transfer Function Model validation	.2-15/
2-147 Common Auxiliary Bearing Configurations	.2-160
2-148 Typical Auxiliary Bearing Mount System [4]	.2-161
2-149 Typical Horizontal Rotor Landing [1]	.2-163
2-150 Vertical Rotor Landing Orbit [2]	.2-163
3-1 Definition of Log Dec Based on Rate of Decay	3-2
3-2 Stability Analysis Flow Chart	3-4
3-3 Fixed Geometry Bearing Schematic	3-8
3-4 High-Speed, Lightly Loaded, Unstable Bearing [1]	3-9
3-5 Low-Speed, Heavily Loaded, Stable Bearing [1]	. 3-10
3-6 Bearing-Induced Shaft Whip and Oil Whirl [1]	3-11
3-7 Frequency Spectrum, Power Turbine Test, 3-axial Groove Bearings [1]	3-12
3-8 Rotor Bearing System Stability, Power Turbine <i>N</i> = 5000 rpm [1]	3-13
3-9 Frequency Spectrum, Power Turbine Test, Double Pocket Bearings [1]	
3-10 Frequency Dependent Stiffness and Damping	. 3-16
3-11 Full Coefficient vs. Synchronous Reduced Tilting Pad Bearing Stability Sensitivity	3-17
3-12 Waterfall Showing Self-Excited Instability	3-18
3-13 High-speed Balance Vacuum Pit Oil Atomization Resulting in Subsynchronous Vibration [3]	3-20
3-14 Single Housing Orifice Design Resulting in Subsynchronous Vibration [3]	3-21
3-15 Spray Bar Evacuated Housing Design [3]	
3-16 Button Spray Design Resulting in Subsynchronous Vibration [3]	3-22
3-17 Squeeze Film Damper Schematic	3-23
3-18 Typical End Seal Arrangements	3-24
3-19 Axial Pressure Profiles of Various Damper Arrangements	. 3-25
3-20 Squeeze Film Damper Coefficients vs. Eccentricity Ratio: Short Bearing Theory (Cavitated) [8]	
3-21 Idealization of Bearing-damper-support Characteristics [6]	

3-22	O-ring Supported Squeeze Film Damper Schematic [2,3]	3-29
3-23	Mechanical Arc Spring Supported Squeeze Damper [12]	3-30
3-24	Squeeze Film Damper Stability Map [7]	3-31
3-25	Re-excitation of Rotor First Critical from Oil Seal Excitation	3-34
3-26	Rotor Tracking Instability from Low-pressure Oil Seal Test	3-35
3-27	Rotor Tracking Instability from Distorted Oil Seal Lip Contact Area	3-35
3-28	Typical Configuration for a Back-to-Back Compressor	3-38
3-29	Typical Configuration for an In-line Compressor	. 3-38
3-30	Typical Configuration for the Last Stage of a Series Flow Compressor Showing the Impeller Eye S	Seal,
	the Inter Stage Seal and a Typical Balance Piston Seal	3-39
3-31	Shunt Line Schematic to Reduce Entry Swirl [8]	3-41
3-32	Typical Swirl Brake Schematic to Reduce Entry Swirl	3-42
3-33	Compressor on Full Load Test: With Inert Gas Showing no Instability at Rotor First Critical Frequ	ency
	[13], with Process Gas Showing Instability from Balance Piston Excitation [5,13]	3-42
3-34	Measured and Predicted Rotordynamic Stability vs. Discharge Pressure for a High Pressure Cent	rifugal
	Compressor [1]	. 3-45
3-35	Comparison of Honeycomb and Hole Pattern Seals [4]	
3-36	Various Hole Pattern Surface Areas Relative to Honeycomb [4]	3-46
3-37	Example Plot of Predicted Rotor Stability as a Function of Damper Seal Clearance Taper [11]	3-47
3-38	Blade Forces Due To Centerline Displacement	3-50
3-39	Shrink Fit Internal Friction and Shaft Material Hysteresis Destabilizing Force [1]	3-53
3-40	Dry Friction Rub Backward Whirl Excitation [1]	3-54
3-41	Entrapped Fluid Cross-coupled Force [1]	3-55
3-42	Differential Heating at Bearing Journal for Synchronous Forward Whirl	3-56
3-43	Predicted and Measured Stability Threshold with and without Bearing Support Models	3-59
3-44	Stiffness Ratio vs. Log Dec for Two Example Centrifugal Compressors	. 3-60
3-45	% Critical Damping vs. Log Dec for Two Example Centrifugal Compressors	3-60
3-46	Sood's General Rotor Stability Criteria [1]	3-62
3-47	Sood/Fulton Empirical Stability Criteria [2]	3-62
3-48	Kirk's Compressor Design Map [4]	3-63
3-49	API Level I Screening Plot	3-64
3-50	Memmott's Compressor Experience Plot—Flexibility Ratio vs. Average Gas Density [8, 9]	3-65
3-51	Memmott's Compressor Experience Plot—Pressure Parameter vs. Flexibility Ratio [8,9]	3-66
3-52	Memmott's Compressor Experience Plot—Bearing Span/Impeller Bore vs. Average Gas Density [8,9] .	3-66
3-53	Memmott's Compressor Experience Plot—Pressure Parameter vs. Bearing Span/Impeller Bore [13,14] .	3-67
3-54	Steam Turbine Leakage Path	3-69
3-55	Typical Resultant Bearing Load Vector Including Partial Arc Admission Steam Forces	3-70
3-56	FCC Expander Critical Speed Map	3-72
3-57	FCC Expander Cross-section	3-74
3-58	FCC Expander Rotor-bearing-support Model	3-75
3-59	Axial Compressor Rotor Construction: Disk-on-shaft Shrink Fit	3-76
3-60	Axial Compressor Rotor Construction: Stacked Disks with Tie Bolts	3-77
3-61	Axial Compressor Rotor Construction: Drum Rotor with Studs	3-78
3-62	Axial Compressor Rotor Construction: Drum Rotor with Tie Bolts	3-79
3-63	High-speed Gearbox Pressure Dam Pinion Bearing	. 3-81
3-64	High-speed Gearbox Pressure Dam Bull Gear Bearing	3-81
3-65	Typical Multi-stage High-pressure Centrifugal Compressor Rotor	3-82
3-66	Overhung Compressor Rotor	3-83
3-67	Pinion Rotors from an Integrally Geared Compressor	3-84

3-68	Forces Exerted on a Whirling Shaft	3-87
3-69	Mode Shapes for Various Support/Rotor Stiffnesses	3-88
3-70	Half Spectrum Plot	3-95
3-71	Forward Precession Vibration	3-96
3-72	Reverse Precession Vibration	3-97
3-73	Full Spectrum—Reverse Precession of 0.5X	3-97
3-74	Shaft Centerline Plot	3-98
3-75	Measured vs. Identified Frequency Response Functions during a Stability Test [7]	.3-101
3-76	Time Transient Waveform from Blocking Excitation during a Stability Test [7]	.3-102
3-77	Estimating Stability from Time Transient Data Using Mechanical Log Decrement [12]	.3-103
SP-9	Level I Screening Plot	.3-110
3-78	Process Compressor Cross-section	.3-113
3-79	Gas Injection Compressor Cross-section	3-113
3-80	Process Compressor Stability Plot	3-117
3-81	Gas Injection Compressor Stability Plot	3-117
3-82	Process and Gas Injection Compressors on Experience Plot	3-118
3-83	AMB System	3-120
3-84	AMB System Aves	3-121
3-04	Stability Analysis/Log Dec Requirements for AMB Systems	3-124
3-86	Example of Sensitivity Transfer Function	3-125
3-00	Sensitivity Function Measurement Locations	3-125
2.00	Sensitivity Transfer Function That Fails to Most the Accontance Criterion	2 1 2 2
J-00	Typical Coupling Stiffness Boundary	.3-120
4-1	Side View of a Tunical Mater/Coar/Comprogram Train	4-2
4-2	Side view of a Typical Motor/Gear/Compressor Train	4-2
4-3	Schemetia Lumned Decemeter Medel for the Meter/Compressor Trein	4-3
4-4	Schematic Lumped Parameter Model for the Motor/Gear/Compressor Train	4-3
4-5	Side view of a Typical Steam Turbine Drive Compressor Train	4-4
4-0	Cohematic Lymnad Devenator Model for the Steem Typical Compressor Train	4-4
4-7	Schematic Lumped Parameter Model for the Steam Turbine Driven Compressor Train	4-5
4-8	A Typical Twin-pinion Integrally Geared Centrifugal Compressor That Should be Modeled as a Bra	ncnea
4.0	System	4-7
4-9	Effective Penetration of a Smaller Diameter Shaft Section into a Larger Diameter Shaft Section	4-8
4-10		4-9
4-11	Examples of Shrunk on Sleeves with and without Relieved Fits	
4-12		4-10
4-13	A Reduced Moment Gear Coupling.	. 4-11
4-14	A Marine-style Diaphragm Coupling	
4-15	A Reduced Moment Disc Coupling	
4-16	Coupling Spacer Torsional Stiffness Model	4-13
4-17	Typical Nonlinear Stiffness vs. Torque Characteristic for an Elastomeric Coupling	4-14
4-18	An Elastomeric Hybrid Coupling (w/Disc Type)	. 4-15
4-19	Temperature-dependent Shear Modulus Curve	4-16
4-20	Cross-sectional View of a Parallel Shaft Speed Increaser	4-18
4-21	Torsional Model of a Parallel Shaft Speed Increaser	. 4-19
4-22	Torsional Model of a Gear Mesh	4-20
4-23	Typical Geometry of a Webbed Motor Rotor and Cross-Section Under the Windings	. 4-22
4-24	Torsional Stiffness Data for Six-Webbed Shaft with Varying Web Thickness [8]	4-23
4-25	Torsional Stiffness and Damping Coefficients of a 930 kW Eight-pole Induction Motor with rated	
	Operation Condition [9]	4-25